

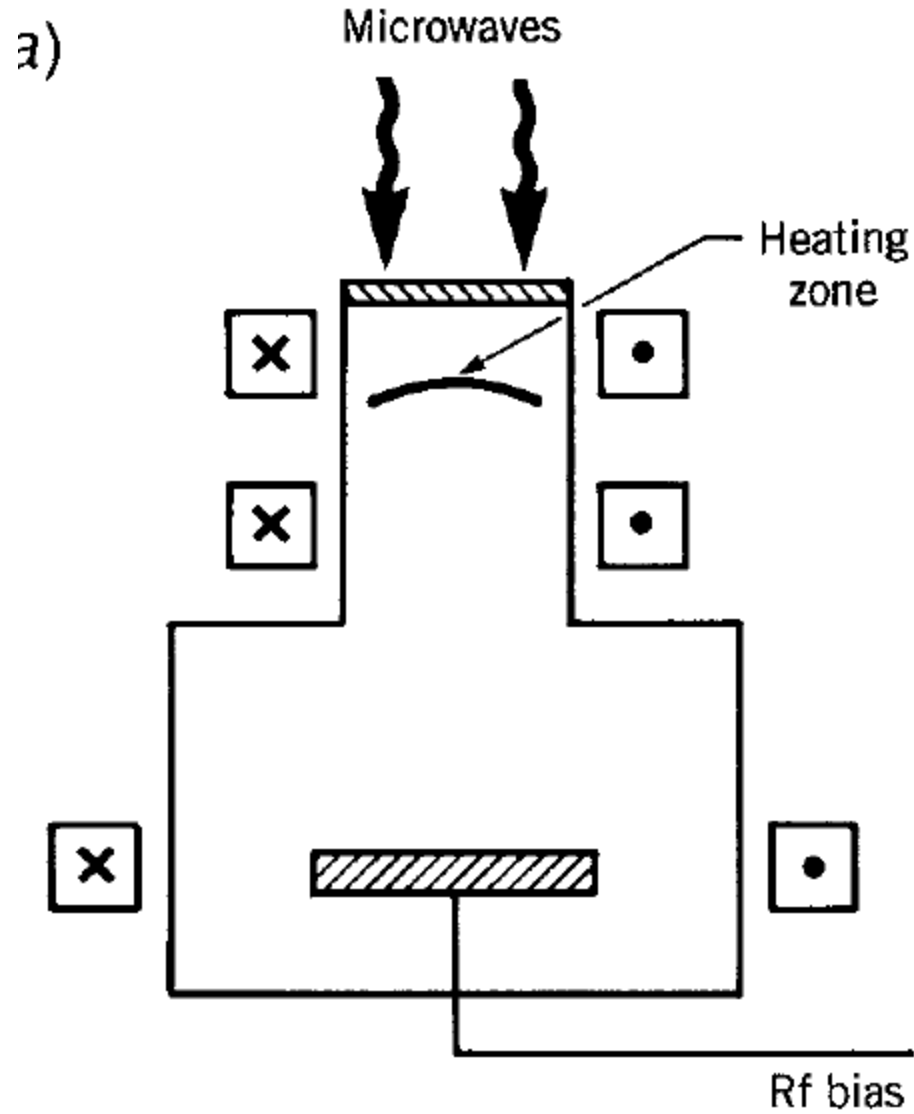
# Лекция 8

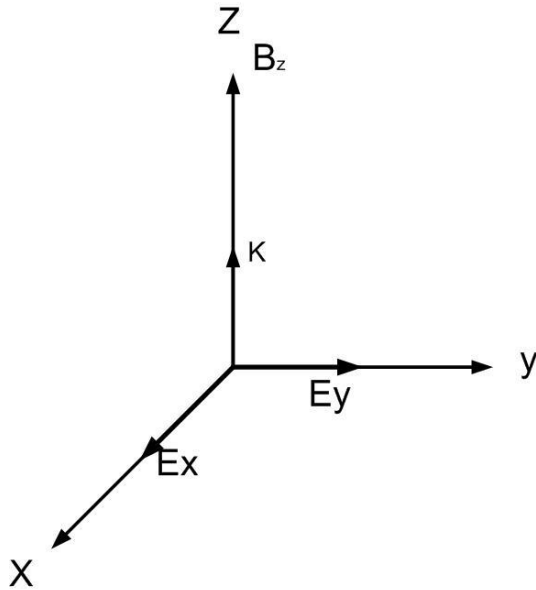
## Разряды в замагниченной плазме.

1. Электронный циклотронный  
резонанс.

2. Геликонные волны

# Электронный циклотронный резонанс





$$\mathbf{E} = E_{x,y} \cdot \exp(-i\omega t)$$

$$\begin{pmatrix} j_x \\ j_y \end{pmatrix} = \frac{\epsilon_0 (\omega_p)^2}{(-i\omega + \nu)^2 + (\omega_c)^2} \cdot \begin{pmatrix} -i\omega + \nu & -\omega_c \\ \omega_c & -i\omega + \nu \end{pmatrix} \cdot \begin{pmatrix} E_x \\ E_y \end{pmatrix}$$

$$\nabla^2 \mathbf{E} - \frac{\omega^2}{c^2} \frac{d^2 \mathbf{E}}{dt^2} = -\mu_0 \frac{d\mathbf{j}}{dt}$$

$$\begin{pmatrix} k^2 & 0 \\ 0 & k^2 \end{pmatrix} \cdot \begin{pmatrix} E_x \\ E_y \end{pmatrix} = \frac{\omega^2}{c^2} \cdot \begin{pmatrix} k_t & -ik_g \\ ik_g & k_t \end{pmatrix} \cdot \begin{pmatrix} E_x \\ E_y \end{pmatrix}$$

1. Право поляризованная волна.

$$E = E_x - iE_y$$

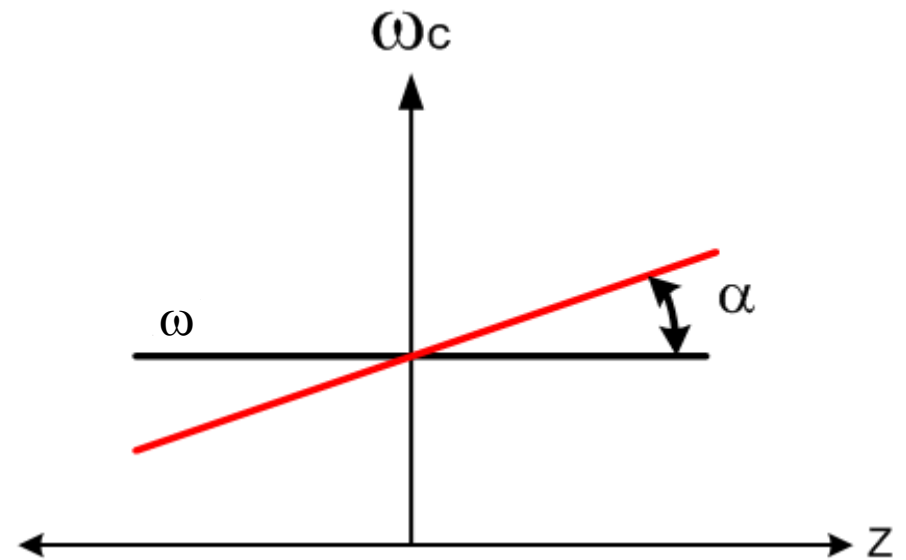
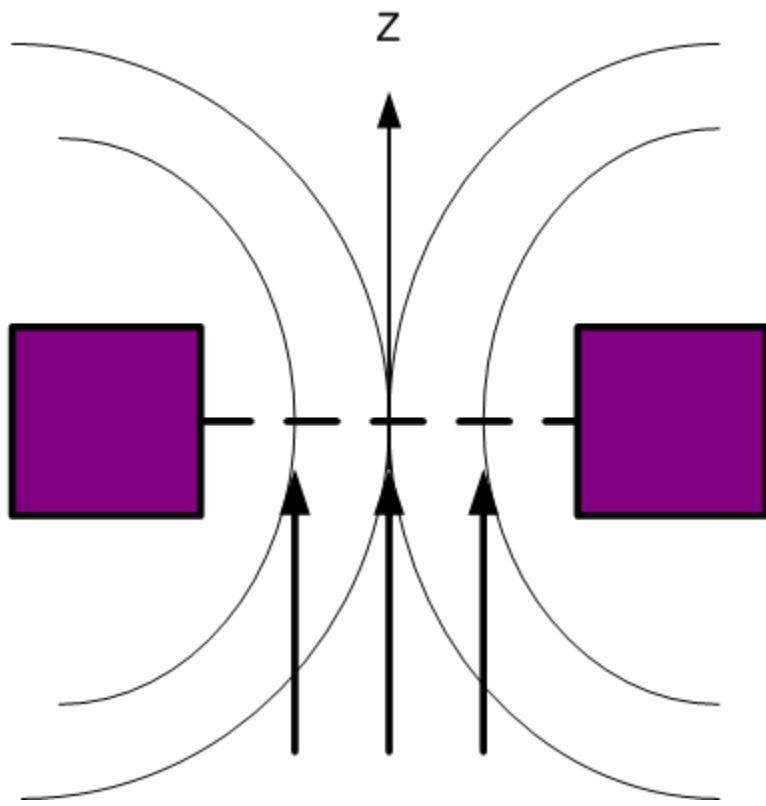
$$(k_r)^2 = \frac{\omega^2}{c^2} \left[ 1 - \frac{(\omega_p)^2}{\omega(\omega - \omega_c)} \right] \quad \omega < \omega_c$$

2. Лево поляризованная волна.

$$E = E_x + iE_y$$

$$(k_l)^2 = \frac{\omega^2}{c^2} \left[ 1 - \frac{(\omega_p)^2}{\omega(\omega + \omega_c)} \right]$$

$$\frac{dv_r}{dt} - i(\omega - \omega_c) v_r = \frac{-e}{m} E_r - \nu v_r$$



$$\omega_c(z) = \omega \cdot (1 + \alpha \cdot z)$$

$$z = v_p \cdot t$$

$$\frac{dv_r}{dt} - i \cdot \omega \cdot \alpha \cdot v_p \cdot t \cdot v_r = \frac{-e}{m} E_r$$

Решение однородного уравнения

$$v_r(t) = A(t) \cdot \exp\left(i \cdot \omega \cdot \alpha \cdot v_p \cdot \frac{t^2}{2}\right)$$

$$\Theta(t) = \omega \cdot \alpha \cdot v_p \cdot \frac{t^2}{2}$$

$$A(T) = A(-T) - \left(\frac{eE}{m}\right) \cdot \int_{-T}^T \exp(-i\Theta(t_1)) dt_1$$

$$v_r(T) \cdot \exp(-i\Theta(T)) = v_r(-T) \cdot \exp(-i\Theta(-T)) - \left(\frac{eE}{m}\right) \cdot \int_{-T}^T \exp(i\Theta(t_1)) dt_1$$

При условии  $T > \tau > \left(\frac{2\pi}{\omega\alpha v_p}\right)^{\frac{1}{2}}$

$$\int_{-T}^T \exp(i\Theta(t_1)) dt_1 = (1 + i) \cdot \left(\frac{\pi}{\omega\alpha v_p}\right)^{\frac{1}{2}}$$

$$\left[ |v_r(T)| \right]^2 = \left[ |v_r(-T)| \right]^2 + \left( \frac{eE}{m} \right)^2 \cdot \frac{2\pi}{\omega\alpha v_p}$$

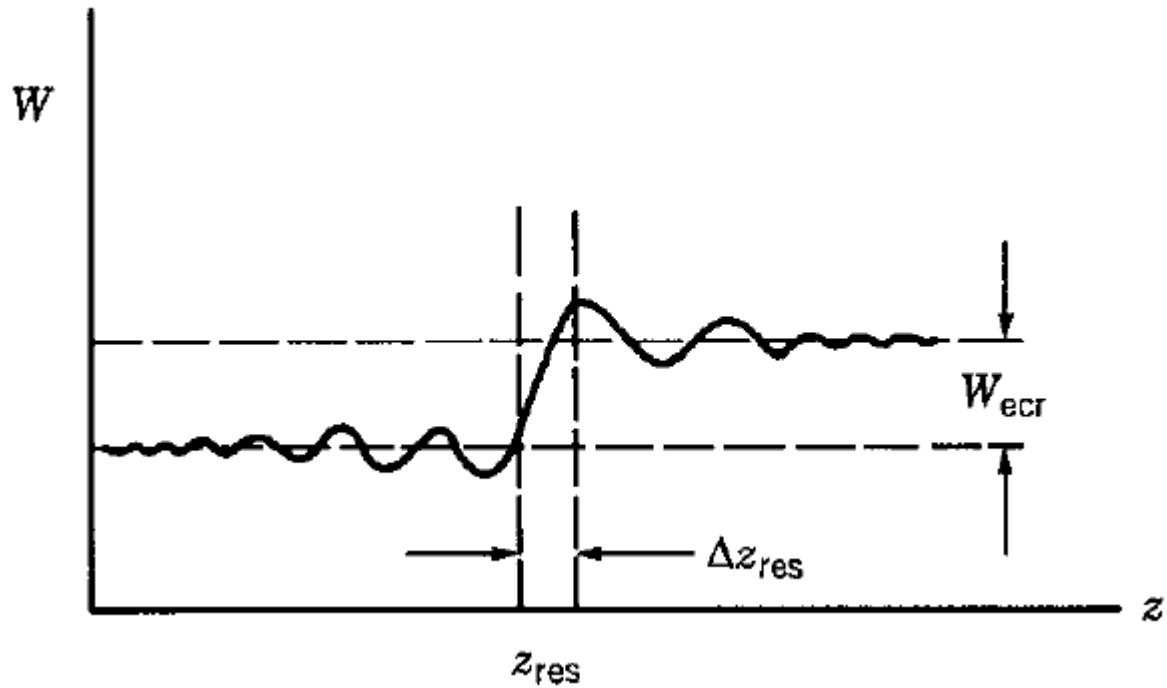
$$W_{\text{ecr}} = \frac{m \cdot \left( |\Delta v_r| \right)^2}{2} = \frac{\pi e^2 E^2}{m\omega\alpha v_p}$$

$$\Delta v_r = \frac{eE}{m} \Delta t_{\text{res}}$$

$$\Delta t_{\text{res}} = \left( \frac{2\pi}{\omega\alpha v_p} \right)^{\frac{1}{2}}$$



$$P = W_{\text{ecr}} \cdot n \cdot v_p = \frac{\pi \cdot n e^2 E^2}{m \omega \alpha}$$



# Геликонные волны.

$$(k_r)^2 = \frac{\omega^2}{c^2} \left[ 1 - \frac{(\omega_p)^2}{\omega(\omega - \omega_c)} \right]$$

$$\omega < \omega < \omega_p$$

$$\omega < \omega < \omega_c$$

$$k^2 = \left( \frac{\omega}{c} \right)^2 \cdot \frac{(\omega_p)^2}{\omega \cdot \omega_c}$$

$$k = \frac{\omega_p}{c} \cdot \sqrt{\frac{\omega}{\omega_c}}$$

$$\lambda = 2 \cdot \pi \cdot \frac{c}{\omega_p} \cdot \sqrt{\frac{\omega_c}{\omega}}$$

$$\omega = 8.5 \cdot 10^7 \quad (13\text{MHz})$$

$$\lambda_0 = 22$$

$$\omega_p = 2 \cdot 10^{10} \quad (n_e = 10^{17})$$

(m)

$$\lambda = 0.17$$

$$f_c = 2.8 \cdot 10^8 \quad (100\text{Gs})$$

## Поглощение геликонной волны

$$k^2 = \left(\frac{\omega}{c}\right)^2 \cdot \left[ 1 - \frac{(\omega_p)^2}{\omega \cdot (\omega - \omega_c + i \cdot \nu)} \right]$$

$$k^2 = \left(\frac{\omega_p}{c}\right)^2 \cdot \frac{(\omega_c - \omega + i\nu)}{(\omega_c - \omega)^2 + \nu^2} \cdot \omega$$

$$\omega_c > \omega > \nu$$

$$k^2 = \left(\frac{\omega_p}{c}\right)^2 \cdot \frac{\omega}{\omega_c} \cdot \left( 1 + i \cdot \frac{\nu}{\omega} \right)$$

$$\mathbf{k} = k_r + i \cdot k_{im}$$

$$k^2 = (k_r)^2 - (k_{im})^2 + 2 \cdot i \cdot k_r \cdot k_{im}$$

$$(k_r)^2 - (k_{im})^2 = \operatorname{Re}(k^2) = \left( \frac{\omega_p}{c} \right)^2 \cdot \frac{\omega}{\omega_c}$$

$$2 \cdot k_r \cdot k_{im} = \operatorname{Im}(k^2) = \left( \frac{\omega_p}{c} \right)^2 \cdot \frac{\omega}{\omega_c} \cdot \frac{\nu}{\omega_c}$$

$$k_r = \frac{\omega_p}{c} \cdot \sqrt{\frac{\omega}{\omega_c}}$$

$$k_{im} = \frac{1}{2} \cdot \frac{\nu}{\omega} \cdot \frac{\omega_p}{c} \left( \frac{\omega}{\omega_c} \right)^{\frac{3}{2}} = \frac{1}{2} \cdot \frac{\nu}{\omega_c} \cdot k_r$$

$$k_r = \frac{2 \cdot \pi}{\lambda}$$

$$\alpha = \frac{1}{k_{im}} = \frac{2 \omega_c}{\nu \cdot k_r} = \frac{\omega_c \cdot \lambda}{\pi \cdot \nu}$$

$$\alpha > \lambda > \lambda$$

$$\nu = 5 \cdot 10^7 \quad (3\text{mTorr})$$

$$\alpha = 1 \quad \lambda = 0.17$$

Затухание Ландау